

<b>Course Title:</b>				<b>Metric Spaces</b>				
<b>Course Code:</b>				<b>MTL 3233</b>				
<b>Course Coordinator</b>				<b>Dr Himani Arora</b>				
<b>Credits</b>				<b>04</b>				
<b>Evaluation Scheme Total 100 Marks</b>								
<b>Quiz (Total 20 Marks)</b>				<b>Assignment/Project (Total 20 marks) (Minimum Two Assignments or one Project)</b>		<b>Mid-Term</b>	<b>Major Examination</b>	<b>Total</b>
<b>Quiz I (5 marks)</b>	<b>Quiz II (5 marks)</b>	<b>Quiz III (5 marks)</b>	<b>Quiz IV (5 marks)</b>			<b>20 marks) (1 ½ Hour Duration)</b>	<b>(40 marks) (3 Hour Duration)</b>	<b>100 Marks</b>
<b>WEEKS</b>				<b>TOPICS TO BE COVERED</b>				
<b>Week 1</b>				<ul style="list-style-type: none"> <li>• Definition of metric space</li> <li>• Illustration through various examples</li> <li>• Discrete metric space</li> <li>• Pseudo metric space</li> </ul>				
<b>Week 2</b>				<ul style="list-style-type: none"> <li>• Bounded and unbounded metric space</li> <li>• Distance between two sets</li> <li>• Diameter of a set</li> </ul>				
<b>Week 3</b>				<ul style="list-style-type: none"> <li>• Open and closed balls</li> <li>• Interior points and interior of a set</li> <li>• Examples and basic results</li> <li>• Open set</li> </ul>				
<b>Week 4</b>				<ul style="list-style-type: none"> <li>• Neighborhood of a point</li> <li>• Limit point of a set</li> <li>• Closure of a set</li> <li>• Closed set</li> <li>• Examples and basic results</li> </ul>				
<b>Week 5</b>				<ul style="list-style-type: none"> <li>• Boundary points</li> <li>• Exterior points</li> <li>• Subspace of a metric space</li> <li>• Results</li> </ul>				
<b>Week 6</b>				<ul style="list-style-type: none"> <li>• Sequences and sub sequences in a metric space</li> <li>• Cauchy sequences</li> <li>• Examples and results</li> </ul>				
<b>Week 7</b>				<ul style="list-style-type: none"> <li>• Definition of complete metric spaces</li> </ul>				

	<ul style="list-style-type: none"> <li>• Illustration through examples</li> </ul>
<b>Week 8</b>	<ul style="list-style-type: none"> <li>• Relation between completeness and closedness</li> <li>• Basic results</li> </ul>
<b>Week 9</b>	<ul style="list-style-type: none"> <li>• Cantor's intersection theorem</li> <li>• Completion theorem</li> <li>• Dense sets</li> </ul>
<b>Week 10</b>	<ul style="list-style-type: none"> <li>• Separable spaces</li> <li>• No where dense sets</li> <li>• Baire Category theorem</li> </ul>
<b>Week 11 (17<sup>th</sup> -21<sup>st</sup> March, 2025)</b>	<b>Mid-Term</b>
<b>2<sup>nd</sup> April, 2025</b>	<b>Showing of Mid-Term Answer Sheets</b>
<b>Week 13</b>	<ul style="list-style-type: none"> <li>• Cover of a Metric space</li> <li>• Compact metric spaces</li> <li>• Compact sets and their criterion</li> </ul>
<b>Week 14</b>	<ul style="list-style-type: none"> <li>• Properties of Compact sets</li> <li>• Relation between compactness, completeness and closedness</li> <li>• Finite intersection property</li> </ul>
<b>Week 15</b>	<ul style="list-style-type: none"> <li>• Bolzano Weirstrass property</li> <li>• Sequential compactness</li> <li>• Totally bounded spaces</li> <li>• Continuous functions between two metric spaces.</li> </ul>
<b>Week 16</b>	<ul style="list-style-type: none"> <li>• Characterization of continuous functions</li> <li>• Continuous functions on compact spaces</li> <li>• Uniform continuous function</li> </ul>
<b>Week 17 (5<sup>th</sup> -9<sup>th</sup> May, 2025)</b>	<b>Revision Week</b>
<b>Week 18 (13<sup>th</sup> – 22<sup>nd</sup> May, 2025)</b>	<b>Major Examinations</b>
<b>29<sup>th</sup> May, 2025</b>	<b>Showing of Major Exams Answer Sheets</b>

**Course Outcomes: On completion of this course, the student will be able to:**

**CO1: learn various natural and abstract formulations of distance on the sets of usual or unusual entities. Become aware one such formulations leading to metric spaces.**

**CO2: understand the basics notions from metric spaces, namely, completeness and compactness of a metric space**

**CO3: know about Banach fixed point theorem, whose far-reaching consequences have resulted into an independent branch of study in analysis, known as fixed point theory.**

**Recommended Books:**

1. S. Shirali and H.L. Vasudeva, Metric Spaces, Springer, 2<sup>nd</sup> edition, 2011.
2. S. Kumaresan, Topology of Metric Spaces, Alpha Science, 2005.
3. P.K. Jain and Khalid Ahmad, Metric Spaces, Alpha Science, 2004.

Calendar of Quizzes/Assignment etc. to be provided as per below details and exact dates to be fixed in consultation with other course coordinators to avoid overlap of Quizzes of different courses.

Component	Date
Quiz-I	27 <sup>th</sup> -31 <sup>st</sup> , January 2025
Quiz-II	24 <sup>th</sup> -28 <sup>th</sup> February, 2025
Assignment-I	10 <sup>th</sup> -12 <sup>th</sup> February, 2025
Mid-Term	17-21 <sup>st</sup> March, 2025
Assignment-II/ Project Submission	21 <sup>st</sup> – 24 <sup>th</sup> April, 2025
Quiz-III	7 <sup>th</sup> – 11 <sup>th</sup> April, 2025
Quiz-IV	28 <sup>th</sup> April-2nd, May, 2025
Major Exam	13 <sup>th</sup> – 22 <sup>nd</sup> May, 2025

**Note:**

1. One surprise Quiz may be fixed out of Quiz-II, Quiz-III or Quiz-IV.
2. In case of any deviation in evaluation methodology for courses such as AEC/VAC/SEC shall be mentioned accordingly. Thus, same shall be approved by the next BOS of school if not done earlier.

**Signature of Course Coordinator :**